

## THIRD SPACE LEARNING

Specialist 1-to-1 maths interventions and curriculum resources

## Rapid Reasoning

## Year 6 | Week 1

This is the first week that children will have met Rapid Reasoning in Year 6 and therefore they may find it more challenging to begin with.

As we are at the start of Year 6, the majority of the objectives covered this week involve Year 5 content. The Year 5 objectives that are re-introduced this week focus on place value.

Year 6 objectives introduced in a reasoning context for the first time this week include:

- reading, writing, ordering and comparing numbers up to 10,000,000
- rounding numbers to any degree of accuracy.

We hope your class enjoys this first week of Rapid Reasoning!

Q1
a Write the number three million, two hundred and forty thousand, four hundred and three in digits.
$\qquad$
b Write the number 456,802 in words.
$\qquad$
$\qquad$
1 mark

Circle the prime numbers below.

| 1 | 2 | 4 | 15 | 19 | 23 | 242 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

2 marks

## Q1

a Write the number three million, two hundred and forty thousand, four hundred and three in digits.

$$
3,240,403
$$

$\qquad$
b Write the number 456,802 in words.

## Four hundred and fifty six

thousand, eight hundred
and two.
$\qquad$
$\qquad$

Q2 Freddie's Fairground has 4,568 visitors on Friday, 10,832 visitors on Saturday and 6,789 visitors on Sunday.

```
How many visitors did Freddie's
Fairground have altogether between
Friday and Sunday?
```

1 mark

Circle the prime numbers below.

2 marks

|  | Requirement | Mark | Additional guidance |
| :---: | :--- | :---: | :--- |
| Q1a | $3,240,403$ | 1 | Commas are not required for the award <br> of the mark. |
| Q1b | Four hundred and fifty six thousand, <br> eight hundred and two. | 1 | Commas, capitalisation and hyphens are <br> not required for the award of the mark. <br> Spellings must be phonetically plausible. |
| Q2 | 22,189 | 1 | 2 |
| Q3 | Award TwO marks for 2, 19 and 23 circled. <br> Award ONE mark for: <br> two correct numbers circled and NO incorrect <br> numbers circled <br> three correct numbers circled, with ONE additional, <br> incorrect numbers circled. | Yumber above two is composite (i.e. non prime). |  |

Q1



Choose from the cards above to complete the calculations. You won't need to use them all.


2 marks
Q2


Round 4,594 to the nearest 10 .
$\qquad$
1 mark

## Q2

b Round 496,843 to the nearest ten thousand.
$\qquad$

| Day | Visitors to <br> Art Museum | Visitors to <br> Science Museum |
| :--- | :--- | :--- |
| Monday | 4,594 | 4,503 |
| Tuesday | 8,832 | 6,842 |
| Wednesday | 3,043 | 9,832 |

a On which day(s) did the Art Museum have more visitors than the Science Museum?
$\qquad$
b Which museum had the most visitors altogether between Monday and Wednesday?

Q1


Choose from the cards above to complete the calculations. You won't need to use them all.


Q2
2 marks
a Round 4,594 to the nearest 10.
$\qquad$
4,590

## Q2

b Round 496,843 to the nearest ten thousand.
500,000
b Which museum had the most visitors altogether between Monday and Wednesday?

Science Museum

Q3

| Day | Visitors to <br> Art Museum | Visitors to <br> Science Museum |
| :--- | :--- | :--- |
| Monday | 4,594 | 4,503 |
| Tuesday | 8,832 | 6,842 |
| Wednesday | 3,043 | 9,832 |

a On which day(s) did the Art Museum have more visitors than the Science Museum?more visitors than the Science Museum?

Monday AND Tuesday

|  | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| Q1 | Award TWO marks for correctly completing all boxes. $\begin{aligned} 4,594 \div 100 & =45.94 \\ 33,832 \times 10 & =338,320 \\ 54.3 \times 100 & =5,430 \\ 432.4 \times 10 & =43.24 \end{aligned}$ <br> Award ONE mark for the correct completion of THREE boxes. | 2 |  |
| Q2a | 4,590 | 1 | Commas are not required to be present |
| Q2b | 500,000 | 1 | in answers for |
| Q3a | Monday AND Tuesday | 1 | BOTH must be recorded for ONE mark. |
| Q3b | Science Museum | 1 | Accept any unambiguous indication (i.e. Science). |

Q1 Complete these number sentences so that they are correct.

$$
\begin{aligned}
6,843 \times 100 & =\square \\
6,943 \div 1,000 & =\square
\end{aligned}
$$

Q2 Evie has these digit cards:


She makes them into a six-digit number.

- It is larger than 300,000 but smaller than 400,000.
- It has four tens but no thousands.
- It has twice as many ten thousands and tens.
- The digit in the ones place is smaller than the digit in the tens place.

What number has Evie been thinking of?

Q3 Complete the drawing so that it has ONE line of symmetry.


Q1 Complete these number sentences so that they are correct.

$$
\begin{aligned}
6,843 \times 100 & =684,300 \\
6,943 \div 1,000 & =6.943
\end{aligned}
$$

Q2 Evie has these digit cards:


She makes them into a six-digit number.

- It is larger than 300,000 but smaller than 400,000.
- It has four tens but no thousands.
- It has twice as many ten thousands and tens.
- The digit in the ones place is smaller than the digit in the tens place.

What number has Evie been thinking of?

$$
3: 8: 0,5: 4: 2
$$

|  | Requirement | Mark | Additional guidance |
| :---: | :---: | :---: | :---: |
| Q1 | Award ONE mark for EACH correctly completed calculation. $\begin{aligned} 6,843 \times 100 & =684,300 \\ 6,943 \div 1,000 & =6.943 \end{aligned}$ | 2 | Commas are not required for the award of the marks. Ensure decimal points are clear. |
| Q2 | Award TWO marks for all six digits correctly placed. <br> 3 <br> 8 <br> 0 <br> 5 <br> 4 <br> 2 <br> Award ONE mark for four or more digits correctly placed. | 2 | Do NOT award any marks if: <br> - digits are duplicated <br> OR <br> - digits are used that were not provided in the question. |
| Q3 |  | 1 | Accept slight deviance from marked points. <br> It is worth noting that in SATs papers, any points more than 2 mm out may lead to the mark not being awarded. |

What are examiners looking for?
Q1 Complete these number sentences so that they are correct.

$$
\begin{aligned}
6,843 \times 100 & =684,300 \\
6,943 \div 1,000 & =6.943
\end{aligned}
$$

Why are we asking this question?

This question is designed to test children's ability to multiply and divide by 10,100 and 1,000 . Specifically, we are looking to see if children can identify and apply any generalisations they may have made about dividing and multiplying by 10 , 100 and 1,000 (i.e. to divide by 1,000 you move the digits three places to the right).

## What common errors do we expect to see?

Children can confuse the generalisations/rules they have learnt. For example, dividing by 1,000 by moving the digits to the left rather than right (giving the answer 694, 300) or by moving only two places to the right when dividing by 1,000 (giving the answer 69.43). These common errors mean it is really important that children have a true conceptual understanding of any generalisations they make, rather than these simply being 'taught' and 'memorised' as this often leads to children misremembering or misapplying such generalisations/rules.

## Children can incorrectly think that to divide by 1,000

 they remove 3 digits. They would therefore give the answer of 6 . If children are first exposed to dividing by 10,100 or 1,000 by dividing multiples of $10 / 100 / 1,000$ then they often incorrectly generalise that to divide by $10 / 100 / 1,000$ they remove 0 s and then incorrectly think they just remove a certain number of digits.
## How to encourage children to solve this question

When dividing or multiplying by 10,100 or 1,000 , children should be encouraged to draw their own place value grid, like the one shown below.

| HTh | TTh | Th | H | T | O | $\cdot$ | $t$ | $h$ | th |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 6 | 9 | 4 | 3 | $\cdot$ |  |  |  |

They can then use this to help them solve the questions, knowing the generalisations that they have made themselves through your teaching about the direction and number of places that the digits move in.
"To divide by 1,000 I move the digits three places to the right."

| HTh | TTh | Th | H | T | O | $\cdot$ | $t$ | $h$ | th |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 6 | 9 | 4 | 3 | . |  |  |  |
|  |  |  |  |  | 6 | . | 9 | 5 | 4 |

It is important that children remember that the decimal place does not move, and that 0 is a place holder, and therefore fills any 'gaps' in the number.

Remember, when teaching multiplying and dividing by 10,100 and 1,000 it is important that children experience this conceptually, using a mixture of place value grids as well as place value manipulatives, so that they can see and understand why the digits move in the ways they do.

Q1 Draw lines between the fractions that are equivalent.

| $\frac{3}{4}$ | $\frac{12}{80}$ |
| :--- | :--- |
| $\frac{6}{16}$ | $\frac{12}{32}$ |
| $\frac{5}{8}$ | $\frac{10}{24}$ |
| $\frac{5}{12}$ | $\frac{27}{36}$ |
| $\frac{3}{20}$ | $\frac{15}{24}$ |

2 marks
Q2 Marley says, " $8,849,842$ rounded to the nearest thousand is $8,849,000$."

## Explain why Marley is incorrect.



a How far had the car travelled by 1 pm ?

## km

b The car doesn't move during two periods of the day.

## Between which two periods of time does

 the car not move?$\qquad$ to
to

Q1 Draw lines between the fractions that are equivalent.


2 marks

Q2 Marley says, " $8,849,842$ rounded to the nearest thousand is $8,849,000$."

## Explain why Marley is incorrect.



Q3 Distance travelled during car journey

a How far had the car travelled by 1 pm ?

$$
45 \quad \mathrm{~km}
$$

b The car doesn't move during two periods of the day.

## Between which two periods of time does

 the car not move?10 am
2 pm
to
to $\frac{11 \mathrm{am}}{3 \mathrm{pm}}$

|  | Requirement | Mark | Additional guidance |
| :---: | :--- | :---: | :--- |
| Q1 | Award TWO marks for all five lines correctly drawn <br> as shown below. <br> $\frac{3}{4}$ <br> $\frac{6}{16}$ <br> $\frac{5}{8}$ <br> $\frac{5}{12}$ | 2 |  |
| Q2 | Award ONE mark for three correctly matched pairs <br> of fractions. | Correctly identified that: <br> BOTH the hundreds place has the digit 9 in it, and this <br> means that the number needs to be rounded up <br> AND <br> as the thousands place has a digit 9 in it, rounding up <br> the thousands place requires the value of the <br> ten thousands place to change (ie. from 4 to 5) | 1 |

Q1 Josh has drawn a square. Each side is 7.5 cm .
What is the perimeter of the square?


1 mark

Q2 Complete the table below.

|  | Rounded to <br> the nearest ten | Rounded to <br> the nearest <br> thousand |
| ---: | :--- | :--- |
| 496,609 |  |  |
| $4,768,499$ |  |  |
| 895 |  |  |

Q3


What is the value of angle $a$ ?

$$
\text { Angle } a=\quad \circ
$$

Q1 Josh has drawn a square. Each side is 7.5 cm .
What is the perimeter of the square?
30 cm

1 mark

Q2 Complete the table below.

|  | Rounded to <br> the nearest ten | Rounded to <br> the nearest <br> thousand |
| ---: | ---: | ---: |
| 496,609 | 496,610 | 497,000 |
| $4,768,499$ | $4,768,500$ | $4,768,000$ |
| 895 | 900 | 1,000 |

Q3


What is the value of angle $a$ ?

$$
\text { Angle } a=\quad 128 \quad \circ
$$

|  | Requirement |  |  | Mark | Additional guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Q1 | 30 cm |  |  | 1 |  |
| Q2 | Award TWO marks for a correctly completed table, as shown below: |  |  | 2 | Commas are NOT required to be present in answers for the award of marks. |
|  |  | Rounded to the nearest ten | Rounded to the nearest thousand |  |  |
|  | 496,609 | 496,610 | 497,000 |  |  |
|  | 4,768,499 | 4,768,500 | 4,768,000 |  |  |
|  | 895 | 900 | 1,000 |  |  |
|  | Award ONE mark for FOUR or more correctly completed cells. |  |  |  |  |
| Q3 | $128^{\circ}$ |  |  | 1 |  |



## THIRD SPACE <br> LEARNING

Specialist 1-to-1 maths interventions
and curriculum resources

## Rapid Reasoning

## Do you have a group of pupils who need a boost in maths this term?

Each pupil could receive a personalised lesson every week from our specialist 1-to-1 maths tutors.

- Raise attainment
- Plug any gaps or misconceptions
- Boost confidence


## Speak to us:

thirdspacelearning.com02037710095
hello@thirdspacelearning.com

THIRD SPACE LEARNING

